Rising Fourth-Grade Students’ Understanding of Fraction Equivalence

Methodology

- Students: Dalton, Will, Carol, and Camilla just finished third grade and were advancing to fourth grade. Students had a 100% participation rate during the ten-week study involving two interviews and seven one-hour lessons. Lessons were video recorded and transcribed for analysis. Instruction focused on fraction equivalence and comparison.

Key Item 1:
In key item one, students were asked what fraction of the rectangle was shaded. Students then had to explain if they believed that 1/4 of the rectangle was shaded.

Key Item 2:
In key item two, students were to say which portion of each rectangle was shaded. They were also to explain if the fractions shown by the shaded areas were equivalent.

Key Item 3:
In key item three, students were shown figures representing partially eaten candy bars. They were to order from least to most eaten, find the fraction eaten, write the fraction multiple ways, and show multiple ways to indicate one-half.

Literature Review

- The diagram to the left shows the learning progression (Confrey et al., 2012) that guided our research. Our main focus was Common Core standards 4.NF.1 and 4.NF.2.


Instructional Cycle

- We utilized this cycle multiple times over the course of the study to create lessons that targeted our learners’ needs.

Empirical Teaching and Learning Trajectory:

Initial Assessment Results

Key Item 1:
All four students were able to recognize fractions from a visual representation in key item one. Three of the four students agreed that 1/4 and 3/12 were equivalent. Dalton gave a partial explanation, saying they were the same because “3 x 4 is 12.” Carol’s partial explanation for them being equivalent was “because 3/12 is the same as 1/4.” Will did not think the fractions were equivalent saying “there was twelve boxes in there, and she said they were just four boxes in there. And then she said there was one shaded and there was three shaded.” Will’s reasoning suggested he did not believe fractions with equivalent denominators were equivalent.

Key Item 2:
For this key item, two of the students used part-whole reasoning to explain their thinking. Camilla said, “because the fraction is up in the picture, so that’s four squares but three of them are shaded and one wasn’t so it’s three out of four.” Will was not able to recognize equivalent fractions. He said that 3/4 and 9/12 were not equivalent because “one has like short boxes and the other one has long boxes.”

Key Item 3:
All four of the students were able to accurately compare the fractions and order them from least to greatest.

Lessons 1 and 2

During our first lesson we wanted to gauge the children’s understanding of fractions. We had students recognize fractions from a representation then they created their own fractions and drew the corresponding representation. Then we wanted to see how much they understood about fraction equivalence. We had them list examples of fractions that they thought were equivalent. They gave some correct and incorrect responses.

This is an example of a fraction that Carol wrote down. She claimed that they were equivalent fractions because they lined up when she drew them.

During lesson two we continued looking at examples of equivalent fractions. Students were given some correct and incorrect examples. They were asked to determine if they were equivalent or not by shading fraction bars. All answered correctly except for Will. After that we wanted to get an understanding of fraction vocabulary. They had to create their own definition worksheet. They gave vague definitions.

Lessons 3 and 4

For these two lessons we shifted our focus to using fraction strips to further students’ understanding of fraction equivalence. We had them cut out and label the fraction strips. Then they found equivalent fractions using them. For lesson four we wanted to give them a deeper understanding of why fractions are equivalent and that you can see multiple fractions from the same visual representations. We wanted to get away from using unit fractions so we worked with fractions that couldn’t simplify into unit fractions.

These pictures show some chunking and splitting strategies that Will and Carol used in the fourth lesson to find equivalent fractions.

Lessons 5, 6 and 7

For the last three lessons we focused on utilizing different types of manipulatives in order to reinforce ideas of splitting and chunking. This also helped develop students’ reasoning patterns and explanations. In lesson five we used buttons and had the students create fractions using different attributes to group them together.

For lesson six each student was given snap cubes and asked to find the fraction that was represented. Then from that they had to model an equivalent fraction. We noticed that even though they were splitting and chunking they struggled to use vocabulary to explain their thinking. They did not describe the splitting and chunking that they were doing.

For lesson seven we used the snap cubes again in a different situation to prompt them to use the splitting and chunking vocabulary more explicitly. Students worked through an activity sheet and the class explained their thinking and strategies.

Post Assessment Results

Key Item 1:
All four students recognized from the visual representations that 3/12 was shaded. However, only one student said that 1/4 and 1/4 were equivalent. This is different from the previous tests where out of four said they were equivalent. Dalton used part whole reasoning to explain fraction equivalence. He said “simply four sections and one is shaded.”

Key Item 2:
But all but one student was able to recognize the fractions from the two visual representations. Carol miscounted and said 8/12 instead of 8/12. When asked how they knew that the two fractions were equivalent three of the four students said it was because they lined up in the picture. This showed major improvement for Will, who in the pre-interview said they were not equivalent. Camilla explained they were equivalent by saying “because 3 times 3 is 9 and 4 times 3 equals 12.”

Key Item 3:
All four students were able to accurately compare fractions with like denominators. When asked to come up with other names for the fractions Carol used the splitting strategy (she said “split them in half, then blocks are shaded and there are 12 blocks.” This was her explanation as to why 2/6 and 4/12 were equivalent.

Reflection and discussion:
Students struggled with creating equivalent fractions that could not be halved. Students were not able to recognize fractions such as 3/12 and 1/4 as equivalent because 1/4 is not half of 3/12. Splitting and chunking instruction resulted in students wanting to only double or half given fractions. We found learning progression 3.NF.3b, “Recognize and generate simple equivalent fractions and explain using models” to be the most difficult for our students. Students can be helped with this standard through the use of discrete manipulatives. This takes away students’ ability to rely on doubling a fraction to get an equivalent fraction. When students received a visual representation of a fraction with an odd denominator using snap cubes students realized they were unable to “double” the denominator by cutting the cubes in half and deemed it impossible to find and equivalent fraction due to the odd denominator. This forced students out of their comfort zone and directed them toward exploring the idea of splitting fractions into groups larger than halves. While our students were unable to master this concept during the study, they still gained deeper conceptual understanding of creating equivalent fractions.